Development of a Cone CVT by SDPD and Topology Optimization
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Abstract
The automotive industries have undergone a massive change in the last few decades. Nowadays, automotive industries and OEM manufacturers implement various innovative ideas to ensure the desired comfort while minimizing the cost, weight, and manufacturing time. Transmission system plays a major role in the aforementioned items. This paper aims to develop a conical roller with belt Continuously Variable Transmission (CVT) System by employing the System Driven Product Development (SDPD) approach and topology optimization of its traditional design. Furthermore, this paper explains the design steps of the CVT and its advantages and limitations compared with the other automatic transmission systems.

Introduction
Nowadays many automobile industries, as well as customers, consider Continuously Variable Transmission (CVT) system as the primary transmission over the conventional manual gearboxes and epicyclic gear train due to its higher fuel efficiency, wider torque range, and smoother start-up and acceleration [1,2]. CVTs work on the same principle as a conventional manual transmission system works. In other words, in a conventional transmission system, different pitch-circle diameters of the input and output gears lead to different gear ratios. Whereas the infinitive number of different diameters of the input and output pulleys/cones result in continuous torque ratios in CVT. CVT has been a popular transmission system among many automobile industries such as Nissan, Audi, Chevrolet, Honda, Ford, etc. CVT with metal pushing belt and variable pulleys is the most familiar and mostly used CVT in the current automotive industry. This type of CVT transmits the torque through a number of metal blocks, which are placed on one another and pushing each other. The variable pulleys make continuous compatibility between the engine performance map of a car and the external load. This enables the car to use the optimized function of the engine. This type of CVT significantly decreases fuel consumption and improves the acceleration compared with the traditional one [3]. However, this type of CVT suffers from the complex mechanism, distortion of the pulleys, and frequent abrasion in the pulleys surfaces. The other types of CVTs are also hampered predominantly by the low efficiency, disability to transfer high torque, and significant weight. For instances, the spherical CVT is not suitable for high torque applications because of the slippage possibility and the toroidal CVT has a complex design and thus, it has a higher manufacturing cost [4]. This paper focuses on one of the other less frequent types of CVT, known as the cone CVT. A cone CVT uses two conical rollers instead of pulleys and it transmits the power through a belt/ring. Different diameters of the conical rollers result in different torque† ratios. This type of CVT provides infinitive torque ratios, such as the CVT with variable pulleys, which makes it superior compared with the manual and automatic epicyclic transmission systems. The possibility of elimination of hydraulic control system, low number of parts, simple clamping (for shifting mechanisms and control unit), low tolerance requirements, and low shifting power with electromechanical actuation are some of the advantages of the cone CVT over the one with variable pulleys. Furthermore, less manufacturing cost, easier to maintain, and a less possibility to distort due to the transmission of high torque are the other advantages [5, 6].

Börner in 2009 [5] developed the cone-ring CVT, called KRG (Fig. 1), for a wide performance spectrum. His work shows that a cone CVT can design and work in a purely mechanical approach, which makes the control system and mechanism simple and more robust, decrease the number of components, and eliminate the need to the hydraulic system. The aforementioned items significantly reduce manufacturing, maintenance, and repair costs and improve efficiency. Elimination of hydraulic pump to control the components movement shortens the unwanted delay in the shifting process of the involved dynamic systems.

The shifting mechanism in the cone CVT is much simpler than the one with variable pulleys. Fig. 2 shows one of the employed shifting mechanism for a cone CVT [5]. In this mechanism, an input cone (1), an output cone (2) are connected to each other through a transfer ring (3), which can be placed around the input or output cone. Changing the diameter and angle of the cones adopt the start-up and overdrive ratio, as well as the ratio, spread according to the vehicle requirements and installation space. The required clamping force is obtained through the axial displacement of the output cone. A mechanical torque sensor (4) transforms the output torque into an axial pressure force with very high efficiency [5]. Any cone CVT may utilize this mechanism for changing the torque ratio. However, this

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type of CVT has not been taken into consideration for a while by scholars because of some disadvantages/drawbacks including a considerable weight and large volume of the conical roller compared with the CVT with variable pulleys or an automatic transmission system. This type of CVT also suffers from low efficiency because of the slipping issue and the limitation to transfer high torque [6]. However, its excellent benefits such as simple mechanism, less production cost, the non-hydraulic control system, etc. attract scholars and car manufacturers again nowadays. The purpose of this paper is to eliminate these limitations by introducing a new topology optimized design for the CVT and using System Driven Product Development (SDPD) (Fig. 3) methodology. Furthermore, this paper illustrates an example of product development using the SDPD approach.

Figure 2: A designed cone-ring CVT with the shifting mechanism

Figure 3: Different phases of the SDPD methodology

SDPD approach focuses on scaling the product development processes by eliminating the conventional document of driven product development and evolving the model-based product development [7, 8]. SDPD approach firstly uses SysML tools for developing the system, which would demonstrate the requirements of the system as well as its external and internal structure. Secondly, it uses a 1D model to simulate the behavior of a system, where you can use to validate the structure of the system. Thirdly, it uses product designing, analysis, and optimization. This phase uses CAD modeling and analysis tools. Lastly, the manufacturing process planner, plant simulation, and manufacturing phases are included. This case study focuses on the first three phases [7].

In this study, one of the requirements of the system is the fuel economy. Our requirement is to get a better fuel economy than the existent epicyclic gear train for the cone CVT. A number of studies investigated the fuel efficiency of different types of CVT. These studies show that one of the major influencing factors for selecting a CVT system over other transmission systems is its better fuel economy because a CVT system is able to perform in the most efficient zone of Brake-specific fuel consumption (BSFC) diagram compared with transmission using fixed gear ratio [1, 9, 10].

Singh, T. and Nair, S.’s review paper corroborates the advantages of CVT over the other transmission systems. Moreover, they normalized the mathematical model of different types of CVTs and compared their efficiency with each other [11].

Previous literature shows cone CVTs have a great fuel efficiency compared with manual and automatic transmission systems as well as other CVTs systems. Srinath N. compared the efficiency and fuel consumption of the cone CVTs with the manual and automatic transmission system in his work. He showed that this type of CVT reduces the fuel consumption more than 17% compared with the manual and automatic transmission systems and the manufacturing cost will be less. However, this work used the traditional design of the cone CVT, which is suitable for a low load application. Moreover, they designed a manual mechanism with a limited range of gear ratios [12]. Recent developments in materials as well as in the optimization methodologies make possible to optimize the CVT for heavy-duty applications such as automobile industry with a functional weight and volume. In a recent project, European commission in 2017 funded a project called KRG-250 to develop a fuel efficient, cost effective cone-ring CVT for European passenger vehicles [13]. The summary of their objectives offers 30% production cost saving, 25% improved efficiency, and up to 30% reduced fuel consumption.

In this work, we try to leverage the power of SDPD methodology by the employment of some intuitive user interfaces in the field of system engineering to develop and optimize a cone CVT and overcome some of the aforementioned drawbacks/gaps in CVT transmission systems. This work exemplifies the optimization procedure by utilization of some common SE software. This procedure may follow to develop any other product and by using any other software with similar functionalities.

**Problem statement**

The automaker’s production rate and the people’s interest in various types of power transmission systems vary in different parts of the world. Many countries including India and European countries prefer a manual transmission system over an automatic one [1, 14]. An automatic transmission system has not been popular in BRIC countries (Brazil, Russia, India, and China) due to various reasons. First, because of the high cost of automatic transmission systems and their low fuel efficiency. Fuel economy has been always a significant factor for customers especially in developing countries while purchasing a car. This is the reason why only a few international automobile manufacturers offer automatic transmission systems, including CVT in these countries. Furthermore, the roads with a good condition and well-organized traffic, which allows a uniform movement with less break. Thus, the gearbox can run at a lower gear ratio for a longer period, without a need to change the gear regularly. These factors decrease the influence of using automatic transmission systems, whose fuel efficiency is less than the manual ones. However, in developing countries such as India, where the roads are not in such good condition, traffic moves at a very slow pace, and frequent downshifts are required, most domestic automakers and costumers prefer a highly economic transmission system. Even though CVT can adjust the gear ratio
precisely with the BSFC profile to increase the fuel efficiency, its high cost hinders the automakers to employ this high efficient transmission system in their products. These factors make a vivid image to illustrate the reasons why the automotive industry needs to develop a new automatic transmission system with a higher fuel economy but with a relatively lower cost. This paper seeks these objectives by the employment of the SPDP methodology and a topology optimization software, namely, OptiStruct-HyperWorks software to optimize the weight and cost of the vehicle’s transmission system while profiting from the theoretically infinite gear ratios.

System design
This paper considers different factors to engineer and optimize the cone CVT. Fig. 4 shows different phases in SDPD methodology to engineer the product.

Figure 4: Selected phases of the SDPD methodology

SysML in action with Cameo systems modeler leverages numerous advantages of Model-Based Systems Engineering over Document Based Systems Engineering to design the system. In this phase of SDPD, Cameo employs various diagrams to model the system including the system requirements (Fig. 5), the external and internal structure of the system (Fig. 6), and finally the operation of the system. The first step of SDPD is to identify the stakeholder needs and derive requirements of the system through those needs. MBSE enables us to create a requirements model in a requirement diagram. Fig. 5 demonstrates the requirements model created in Cameo for the system we are trying to develop. This diagram describes the major requirements that the software considers for designing a new cone CVT system. These requirements include fuel economy, an optimized weight, and the same torque range. However, the requirement for fuel economy has already been addressed by the previous literature [7, 11, 12, 15] as well as different types of power flow to expand the gear ratio [1, 10, 16], this work improves the requirement by optimization of a cone CVT system with the same torque ratio but an optimized weight. The 1D simulation of the designed system will calculate the suitable torque ratio in the next section. Furthermore, our system should be able to provide us with a low-torque and high-torque value. In other words, the developed system should be able to operate such as the vehicle former transmission system.

Moreover, fuel economy has always been an influential factor while deciding upon a transmission system for an automobile. One requirement was to develop a transmission system, which provides us with a higher fuel efficiency compared with an epicyclic transmission system. The capability to generate suitable gear ratios directly affects the fuel economy parameter. Thus, choosing a cone CVT, which provides theoretically infinite gear ratios, can fulfill this requirement. As it was already mentioned, this makes possible for the transmission system to adjust the torque ratio in accordance with the BSFC diagram at any moment.

The structure of a system needs to be created in Cameo before moving into the detailed designing or engineering the system. Block Definition Diagram in this software allows us to create a model, which shows the essential parts to satisfy all the system requirements. A design engineer needs to perform a brainstorming and identify these components prior to engineering a system. Reasons behind designing such a system are to identify and evaluate the system requirements, structure, and approximate the cost associated with the system that we are trying to develop. The blocks in Fig. 6 as an instance show the components of the CVT system.

Engineer the system
The next phase of SDPD employs LMS Amesim to simulate the system in a one-dimensional fashion. This simulation reveals the behavior as well as validates a few numbers of requirements of the system before moving forward with the design. In other words, Amesim gives us a platform where we can design the system, provide
input parameters and make sure that the system is able to give us the desired outputs/functions. Fig. 7 shows the simulated powertrain system in Amesim including the engine specifications, vehicle weight, generic CVT dimensions, a clutch, and some sensors as the inputs. The purpose of Amesim simulation here is to make sure that the CVT system in the designed powertrain system is going to satisfy our requirement of getting different desired torque ratios as well as provides us with a full analysis of the generated/required torque values and vehicle speeds at different CVT ratio. This can validate whether or not the CVT can provide the desired functions.

This is one major advantage of the SDPD approach; you can validate the behavior of a system even before designing the component. So, you will know whether it is worth moving forward with the idea or not. For instance, in this case study, we model the CVT structure in Cameo by virtually assembling of the system components. This assists to validate virtually if the designed system is functional and fulfills the requirements, or any additional component or modifications are required to complete the system. Amesim directs us in identifying those issues. Once, we identified all the required components by Cameo then Amesim investigates the system behavior. Amesim requires inputs just as a real car would require an input from the Engine. Engine specifications used for this example are generic. This is just to see the behavior of a system prior to designing the system. After completing the simulation, the required output parameters are derived to evaluate the system.

Furthermore, employment of system engineering helps design engineers to gain the benefits from communication between such software to evaluate different aspects of the designed system. For instance, in this case study, using Amesim makes possible to transfer data to the other Siemens PLM tools such as Star CCM+. This tool enables users to perform 1D or 3D co-simulation to perform CFD or stress analysis on the corresponding component. In many cases, this stage can be repeated in a loop after designing the system to modify the design with the actual values. TCP element, shown in Fig. 7, is a crucial element for transferring the data back and forth.

**Design of components: conical rollers design**

The heart of the CVT system is its conical rollers. This type of transmission system uses two conical rollers, which place in front of each other with the opposite direction (Fig. 9). Fig. 10 shows the primary shape of the rollers. We optimize this part of the CVT in the following sections in order to decrease the weight of the transmission system as one of the other requirements mentioned in Cameo model. This section obtains the primary dimensions of the rollers, according to the exerted forces and other design conditions.

![Figure 7: The powertrain system designed in LMS Amesim and the TCP elements for transferring data to the other Siemens PLM tools](image)

![Figure 8: The Amesim results including the range of torque ratio that the CVT is going to generate, the forces induced on the CVT, and any other desired output associated with the designed system. These results show that the CVT fulfills the requirement.](image)

![Figure 9: A CVT with a belt and conical roller modeled by Creo](image)

![Figure 10: The primary shape of the rollers](image)

We used the specifications of the 2013 Nissan Altima as well as the CVT characteristics achieved in the previous section, to calculate the forces and design the rollers. The vehicle specifications include the power produced by the engine, which is 82 KW and the engine RPM, which is 6000 [17]. Furthermore, the main roller dimensions by considering the optimized torque range are as follows:

- The smaller diameter of the rollers: \( d = 50 \text{ mm} \)
- The bigger diameter of the rollers: \( D = 200 \text{ mm} \)
The length of the rollers: \( L = 200 \text{ mm} \)

The belt exerts different force values at a different diameter of the input roller. For instance, by taking the average diameter of the roller, the velocity of the belt is:

\[
\nu = \frac{\pi DN}{60000} \Rightarrow \nu = \frac{\pi \times 125 \times 6000}{60000} = 39.26 \frac{m}{s}
\]

(1)

In this velocity, the difference of the tight side tension of the belt \((P_1)\) and the slack side tension \((P_2)\) is given as:

\[
P_1 - P_2 = \frac{1000 \rho}{\nu} = \frac{1000 \rho (\frac{d}{39.26})}{2} = 2088.11 \text{ N}
\]

(2)

Center distance between the input shaft and output shaft \((C)\) is equal to 150 mm. Thus, we can obtain the length of the belt:

\[
L = 2C + \frac{\pi (D + d)}{2} + \frac{(D - d)^2}{4C}
\]

\[
L = 730.19 \text{ mm} \cong 731 \text{ mm}
\]

(3)

We can also obtain the wrap angle for the smaller pulley by Eq. 4

\[
\alpha_s = 180 - 2 \sin^{-1} \left[ \frac{D - d}{2C} \right]
\]

(4)

And the wrap angle for the bigger sized pulley by Eq. 5

\[
\alpha_s = 180 + 2 \sin^{-1} \left[ \frac{D - d}{2C} \right]
\]

(5)

As it already mentioned, both rollers are identical, which places in front of each other with opposite direction. At the initial stage, the belt is in contact with the smaller end of the driving roller and the larger end of the driven roller. As the operation starts, the belt will slide along both rollers. In the case of driving roller, the belt would be sliding from the smaller end diameter to the bigger end diameter of the roller. Since the driving roller starts with the end with a smaller diameter, we would have to use the smaller roller wrap angle until it reaches the midpoint of the roller. Length of the roller is 200 mm; hence, 100 mm is its midpoint. At 100 mm length from either side, the wrap angle is 180° for both rollers. From the midpoint to the other end of the driving roller, it will have a greater diameter compared with the driven roller. In that case, the larger wrap angle is required for the driving roller. The wrap angle at the initial stage, when the belt locates at the smaller diameter of the driving roller \((d = 30 \text{ mm})\) and the larger diameter of the driven roller \((D = 120 \text{ mm})\), is equal to

\[
\alpha_s = 180 - 2 \sin^{-1} \left[ \frac{D - d}{2C} \right]
\]

\[
\alpha_s = 180 - 2 \sin^{-1} \left[ \frac{200 - 50}{2 \times 150} \right]
\]

\[
\alpha_s = 120^\circ = 2.09439^c
\]

We can obtain the tension on the tight side of the belt and tension on the slack side of the belt by Eq. 6:

\[
\frac{F_1}{F_2} = e^{\mu \alpha_s}
\]

(6)

Where \(\mu\) is the coefficient of friction and it is considered as 0.35 [18]. Considering Eq.2, the forces can be calculated as:

\[
\frac{F_1}{F_2} = 2.09439 \text{ , } (F_1 - F_2) = 2088.11 \text{ N}
\]

\[
\Rightarrow F_1 = 3996.113 \text{ N}, F_2 = 1908.003 \text{ N}
\]

In order to calculate the belt tensions at different belt positions, the length of the conical roller is divided into 100 nodes with a distance of 2 mm between every two consecutive nodes. The following MATLAB code calculates the belt tensions at each corresponding node. In this code, the symbol \(i\) shows the position of the belt on the roller (from the smaller end of the conical roller), \(F_1\) shows the belt force on the tight side, and \(F_2\) shows the belt force on the slack side. Moreover, \(\alpha\) shows the wrap angle at the corresponding belt position, \(D\) shows the diameter of the driven conical roller wrapped by the belt, and \(d\) shows the diameter of the driven conical roller wrapped by the belt.

\[
P = 82; \quad \text{Do} = 200; \quad n = 6000; \quad \text{do} = 50; \quad \text{L} = 200; \quad \text{theta} = \text{atan((Do - do)/(2*L))}; \quad \text{i} = 2; \quad \text{C} = 150; \quad \text{v} = (\pi * ((\text{do}+\text{Do})/2) * ni)/60000; \quad \text{alpha} = (\text{alpha} \_\text{degree}) * \pi/180; \quad \text{F}2 = \text{Force} \_\text{Difference}(\text{alpha} - 1); \quad \text{F}1 = \text{Force} \_\text{Difference} + \text{F}2; \quad \text{fprintf}\left(\text{Initial} \_\text{F}1 = \%d, \text{ Initial} \_\text{F}2 = \%d\right); \quad \text{while} (i < 201)
\]

\[
\text{d} = \text{do} + 2*(\text{tan}(\text{theta}) * i); \quad \text{D} = \text{Do} - 2*(\text{tan}(\text{theta}) \times i); \quad \text{v} = (\pi * ((\text{d}+\text{D})/2) * n)/60000; \quad \text{Force} \_\text{Difference} = (\text{P} \times 10^3 / \text{v}); \quad \text{if}(\text{D} > \text{d}) \quad \text{alpha} = \pi - (2 * \text{asin}((\text{Do} - \text{do})/(2 * \text{C})))\; \text{else} \quad \text{alpha} = \pi + (2 * \text{asin}((\text{d} - \text{D})/(2 * \text{C}))); \quad \text{end}
\]

\[
\text{F}1 = \text{Force} \_\text{Difference} + \text{F}2; \quad \text{fprintf}(\text{F}1 = \%d, \text{ F}2 = \%d); \quad \text{fprintf}(\text{Initial} \_\text{F}1 = \%d, \text{ Initial} \_\text{F}2 = \%d, \text{ F}1, \text{ F}2); \quad \text{while} (i < 201)
\]

\[
\text{d} = \text{do} + 2*(\text{tan}(\text{theta}) \times i); \quad \text{D} = \text{Do} - 2*(\text{tan}(\text{theta}) \times i); \quad \text{v} = (\pi * ((\text{d}+\text{D})/2) * n)/60000; \quad \text{Force} \_\text{Difference} = (\text{P} \times 10^3 / \text{v}); \quad \text{if}(\text{D} > \text{d}) \quad \text{alpha} = \pi - (2 * \text{asin}((\text{Do} - \text{do})/(2 * \text{C}))); \quad \text{end}
\]

The results provide forces on the conical roller at different diameters. Table 1 shows some of these forces.
We can obtain the final dimensions of the conical roller shown in Fig. 11 by considering the results from previous sections including the optimized torque ratio, the exerted forces, displacement limitations, and the length of the conical roller. We can find the final diameter of the shaft by substituting the torsion moment (Eq. 7) and the bending moment (Eq. 8) in Eq. 9. We selected plain Carbon Steel 40C8 with a tensile strength of 580 MPa and yield strength of 380 MPa as the material for the design of the shaft. Fig. 12 shows the final dimensions, which are 35 mm for the diameter of the shaft, 50 mm for the end of the conical roller with a small diameter, and 200 mm for the end of the conical roller with the bigger diameter.

Table 1: Some forces of the roller obtained by the MATLAB code

<table>
<thead>
<tr>
<th>i (mm)</th>
<th>F1 (N)</th>
<th>F2 (N)</th>
<th>Alpha °</th>
<th>d (mm)</th>
<th>D (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>3996.11</td>
<td>1908.11</td>
<td>120</td>
<td>50</td>
<td>200</td>
</tr>
<tr>
<td>5</td>
<td>3901.23</td>
<td>1813.12</td>
<td>123.28</td>
<td>53.75</td>
<td>196.25</td>
</tr>
<tr>
<td>10</td>
<td>3816.59</td>
<td>1728.48</td>
<td>126.51</td>
<td>57.50</td>
<td>192.50</td>
</tr>
<tr>
<td>15</td>
<td>3740.53</td>
<td>1652.42</td>
<td>129.69</td>
<td>61.25</td>
<td>188.75</td>
</tr>
<tr>
<td>20</td>
<td>3671.74</td>
<td>1583.63</td>
<td>132.84</td>
<td>65</td>
<td>185</td>
</tr>
<tr>
<td>100</td>
<td>3063.14</td>
<td>975.02</td>
<td>180</td>
<td>125</td>
<td>125</td>
</tr>
<tr>
<td>200</td>
<td>2742.9</td>
<td>654.8</td>
<td></td>
<td></td>
<td>50</td>
</tr>
</tbody>
</table>

The Torsion moment is:

\[ M_t = \frac{P \times 60 \times 10^6}{2\pi N} \] (7)

\[ \Rightarrow M_t = \frac{82 \times 60 \times 10^6}{2\pi \times 6000} \Rightarrow M_t = 130507.05 \text{ N-mm} \]

Moreover, the bending moment is:

\[ M_b = (3996.11 + 1908.11) \times 100 \] (8)

\[ \Rightarrow M_b = 590422 \text{ N-mm} \]

Thus, the diameter of the shaft can be obtained by:

\[ d_s^3 = \frac{16}{\pi s_{\text{max}}} \sqrt{(1.1M_t)^2 + (1.1M_b)^2} \] (9)

\[ \Rightarrow d_s = 31.93 \approx 32 \]

By taking the standard dimension the diameter is

\[ d_s = 35 \text{ mm} \]

Figure 11: The layout of the input shaft

The volume of a conical roller is,

\[ V = \frac{1}{3} \pi (R^2H - r^2h) \] (10)

Where, H is the height of a cone with the base radius of 100 mm, h is the height of a cone with a base radius of 25 mm, R is the radius of the larger end of the roller, and r is the radius of the small end of the roller. Thus, the volume is obtained as,

\[ V = 2618020 \text{ mm}^3 = 0.002618020 \text{ m}^3 \]

By considering the density of steel equals to 7850 Kg/m\(^3\) the weight of the conical roller will be:

\[ W = \rho V \] (11)

\[ \Rightarrow W = 20.55 \text{ Kg} \]

Table 2 compares the weight of the newly designed CVT with the previously designed CVT [12]. This weight still can be significantly improved by the employment of optimization methods. We fulfilled this objective in the next section.

Table 2: Comparison of the weight of the newly designed CVT with the traditional design

<table>
<thead>
<tr>
<th>SR. No.</th>
<th>Volume ((\text{m}^3))</th>
<th>Density ((\text{Kg/m}^3))</th>
<th>Mass ((\text{Kg}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(16 \times 10^{-3})</td>
<td>7850</td>
<td>126</td>
</tr>
<tr>
<td>2</td>
<td>(2.6 \times 10^{-3})</td>
<td>7850</td>
<td>20.55</td>
</tr>
</tbody>
</table>

Design optimization

In this step, we are going to optimize the shape of the conical roller in order to reduce the weight while keeping its functionality for transferring the torque using HyperWorks-OptiStruct. We have calculated 200 forces by MATLAB exerted on 100 points at a distance of 2 mm from each other. Thus, we selected the mesh with the size of 2 mm. As Fig. 13 shows, we used tetrahedral meshes for analysis of the model. As Fig. 14 shows to the sake of a safe design, we first analyzed a roller while concentrated loads were inserted instead of the distributed load of the belt on the roller. In this case, we will have a...
contact line between the roller and the belt/ring when the belt moves along the roller. Fig. 15 shows the von Mises stress analysis and Fig. 16 shows the deformation/displacement through the model. This assumption will also help in the optimization phase of the model. Our calculation shows that to transfer the torque, we need to consider at least eight contact lines throughout the roller’s surface to have enough contact points between the belt/ring and the conical roller during rotation. We employed OptiStruct-HyperWorks for all the stress analysis and optimization design in this work.

Figure 13: The meshed conical roller

Figure 14: The applied forces on the nodes of the driving conical roller

Figure 15: Von Mises stress analysis

Figure 16: Deformation/displacement through the driving conical roller

Fig. 17 shows the von Mises stress analysis for the applied forces on the eight different contact lines on the driving conical roller. We assumed all the eight contact lines for analysis of the roller because the roller rotates with a very high rpm and the mechanism for moving the belt may need to change its position very quickly to change the torque ratio. Furthermore, we need all the contact points of the belts with the roller to be able to optimize the shape, the design will be safer, and the structure will be symmetric and stronger.

Figure 17: Von Mises stress analysis for eight contact lines

We obtained the optimized conical rollers (Fig. 18 and Fig. 19) by keeping the outer body as a non-design domain and the inner part as the design domain (Fig. 20). We employed the SIMP optimization methodology, which removed 70% of the total material of a conical roller. Thus, the ultimately generated volume became 30% of the original Volume. This new design also let to eliminate the slipping issue by designing and employing a customized belt to grab the solid outer lines (see Fig. 18). This can significantly improve the efficiency of this type of CVT and enhance the level of the torque transferred by the transmission system.

Figure 18: The optimized driving conical roller

Page 7 of 10

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Thermal abnormalities such as distortion are among the most frequent fabrication process may affect the quality of the fabricated parts [19]. However, the defects and abnormalities generated during the fabrication process widely. Sintering (DMLS) or Selective Laser Melting (SLM) process.

We employed the high strength steel alloy, recognized as ASTM A514. Table 3 shows its specifications.

Table 3: The specifications Comparison between the conical roller before and after topology optimization

<table>
<thead>
<tr>
<th>SR. No.</th>
<th>Volume (m$^3$)</th>
<th>V-M Stress (MPa)</th>
<th>Density (Kg/m$^3$)</th>
<th>S$_{yt}$</th>
<th>Mass (Kg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$2.6 \times 10^{-3}$</td>
<td>231</td>
<td>7850</td>
<td>690</td>
<td>20.55</td>
</tr>
<tr>
<td>2</td>
<td>$1.17 \times 10^{-3}$</td>
<td>268</td>
<td>7850</td>
<td>690</td>
<td>9.185</td>
</tr>
</tbody>
</table>

The optimized design reduced the weight of one conical roller to 10 Kg. Thus, the total weight of the CVT system including two rollers, shafts, keys, stoppers, the mechanism for moving the belt, etc. is less than 50 kg, which satisfies the weight requirements mentioned in Cameo software.

### Manufacturing feasibility

The topology-optimized conical roller possesses a freeform geometry with a complex porous structure. Traditional manufacturing processes are unable to fabricate these types of structures. Alternatively, additive manufacturing (AM) processes are capable of fabrication of complex structures with elaborate features. The automotive industry has been employed the metal AM processes such as the Direct Metal Laser Sintering (DMLS) or Selective Laser Melting (SLM) process widely. However, the defects and abnormalities generated during the fabrication process may affect the quality of the fabricated parts [19]. Thermal abnormalities such as distortion are among the most frequent defects in metal AM [20], which is crucial to avoid in the part with a high rotation speed such as the conical roller. Design of suitable temporary/permanent support structures between the fabricated layers can facilitate the conduction during the fabrication process as well as strengthening the structure and thus, reduce the distortion. The fabricated support structures can also be optimized topologically to not affect the weight of the system significantly [21]. The other way to increase the precision and repeatability of the fabricated conical rollers is to employ online monitoring and control of the process. Several systems have been developing to monitor and/or remove the microstructural and macro-structural defects of the fabricated parts [22-26]. Specifically, the porous structures are at risk of damages more than simple solid structures [27, 28].

Scholars have tried to avoid/diminish these defects by controlling the controllable process parameters such as laser specifications or control the fabrication signatures such as melting pool specifications during the fabrication process [20, 29]. A number of scholars also attempted to derive the optimized process parameters even before printing a part by studying the effects of different parameters on the fabrication process through multi-physics simulation of the printing process [30, 31]. This paper studied the theoretical aspects and the design possibilities of the new cone CVT. The manufacturing repeatability and precision is still under question but the only way passes through AM technology. This manufacturing technology makes possible to fabricate the new design, which increases the overall efficiency of the transmission system. First, the new topology optimized design will decrease the rotational inertia of the rotating parts. Second, it will decrease the production cost and time, from the design phase to manufacturing, because of consuming less material for fabrication of the components and decreasing the total number of parts that need to be assembled.

Moreover, there is no investment in designing and fabricating the necessary tooling and fixtures. As regards to time, we can avoid the delays due to tooling that normally take several weeks of work. Delays are costly and thus, removing those leads to a significant financial benefit. The new design and the fabrication capabilities by AM also help to integrate the rotating input/output shaft with the cones/shifting mechanisms or at least reduce the number of parts by replacement of the ones which made of the same material by one integrated assembly. This will reduce or eliminate cost, time, and quality problems resulting from assembling operations [32].

### Conclusion and future works

This paper demonstrates the ability of System Driven Product Development approach to developing an optimized cone CVT system. The existing CVT designs suffer from a number of disadvantages including the considerable weight of the conical rollers and a limited range of the torque in the cone CVT system, and complex mechanism and high production cost in other CVT types. This work employed an innovative system development approach, SDPD, to develop the cone CVT by defining desired system requirements and evaluating these requirements through predicting system behavior and designing the multi-domain system, before designing the components. The newly designed conical roller, as a major component of the CVT, was optimized using OptiStruct-HyperWorks® software. The optimized rollers result in a significant reduction in weight. Our new design could decrease the weight of the traditional cone CVT by 44.69%. This is while the literature demonstrates a non-topology optimized cone CVT can improve the efficiency by 25%, fuel efficiency by 30% and the production cost by 30%. The new design can surpass the weight efficiency of the current transmission systems in the event that other parts of the CVT system are optimized. Furthermore, it increases the efficiency of the transmission system even more by introducing a new design for the elimination of the slipping issue, reducing the rotational inertia of the rotating components, decreasing the production cost, and decreasing the assembling time. The new design results in an optimum strength-to-weight ratio able to meet functional requirements while minimizing material volume. As the future step, we can optimize the
performance of the CVT system by extending the range of the torque ratio while imposing a weight constraint on the design. The manufacturing feasibility with a high precision machining is questionable but metal AM (Additive Manufacturing) provides a unique way of fabricating the complex structures of the proposed design.

References

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Definitions/Abbreviations

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Full Form</th>
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<tbody>
<tr>
<td>AM</td>
<td>Additive Manufacturing</td>
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<tr>
<td>BRIC</td>
<td>Brazil, Russia, India, and China</td>
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<td>BSFC</td>
<td>Brake-Specific Fuel Consumption</td>
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<tr>
<td>CFD</td>
<td>Computational Fluid Dynamics</td>
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<td>CVT</td>
<td>Continuously Variable Transmission</td>
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<tr>
<td>DMLS</td>
<td>Direct Metal Laser Sintering</td>
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<td>MBSE</td>
<td>Model Based Systems Engineering</td>
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<td>PLM</td>
<td>Product Lifecycle Management</td>
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<td>SLM</td>
<td>Selective Laser Melting</td>
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<tr>
<td>SPDP</td>
<td>System Driven Product Development</td>
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<tr>
<td>TCP</td>
<td>Transmission Control Protocol</td>
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